

6.7 - p.500 11, 13, 17, 43, 51

11.)  $2 \sin^2 \theta - 1 = 0$

$$\frac{2 \sin^2 \theta}{2} = \frac{1}{2} \rightarrow \sin^2 \theta = \frac{1}{2} \rightarrow \sqrt{\sin^2 \theta} = \pm \sqrt{\frac{1}{2}}$$

$$\sin \theta = \pm \frac{1}{\sqrt{2}} \rightarrow \sin \theta = \pm \frac{\sqrt{2}}{2}$$

$$\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

13.)  $\sin(3\theta) = -1$  let  $u = 3\theta$

$$\sin u = -1 \rightarrow u = \frac{3\pi}{2} + 2\pi k \rightarrow \frac{3\theta}{3} = \frac{3\pi}{2} + 2\pi k$$

$$\theta = \frac{3\pi}{6} + \frac{2\pi}{3} k \rightarrow \theta = \frac{\pi}{2} + \frac{2\pi}{3} k$$

$$k = 0 \rightarrow \theta = \pi/2$$

$$k = 1 \rightarrow \theta = \frac{\pi}{2} + \frac{2\pi}{3} (1) = \frac{7\pi}{6}$$

$$k = 2 \rightarrow \theta = \frac{\pi}{2} + \frac{2\pi}{3} (2) = \frac{11\pi}{6}$$

$$\theta = \frac{\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6}$$

17.)  $\sec\left(\frac{3\theta}{2}\right) = -2 \rightarrow \cos\left(\frac{3\theta}{2}\right) = -\frac{1}{2}$  let  $u = \frac{3\theta}{2}$

$$\cos u = -\frac{1}{2} \rightarrow u = \frac{2\pi}{3} + 2\pi k, \frac{4\pi}{3} + 2\pi k$$

$$\frac{3\theta}{2} = \frac{2\pi}{3} + 2\pi k \rightarrow \theta = \frac{4\pi}{9} + \frac{4\pi}{3} k, \theta = \frac{8\pi}{9} + \frac{4\pi}{3} k$$

$$\frac{3\theta}{2} = \frac{4\pi}{3} + 2\pi k \rightarrow \theta = \frac{8\pi}{9} + \frac{4\pi}{3} k$$

$$k = 0 \rightarrow \left[ \frac{4\pi}{9}, \frac{8\pi}{9} \right] \quad k = 1 \rightarrow \left[ \frac{16\pi}{9}, \frac{20\pi}{9} \right] \text{ (too large)}$$

$$43.) \tan \theta = 5 \rightarrow \theta = \tan^{-1}(5) = \underline{1.37 \text{ rad}}$$

\*  $\tan \theta$  is positive in Q1 + Q3

$$2\pi - 1.37 \approx \underline{4.91 \text{ rad}}$$

$$\boxed{\{1.37, 4.91\}}$$

$$51.) 3 \sin \theta - 2 = 0$$

$$\frac{3 \sin \theta}{3} = \frac{2}{3}$$

$$\sin \theta = \frac{2}{3} \rightarrow \theta = \sin^{-1}\left(\frac{2}{3}\right) = \underline{0.73 \text{ rad}}$$

$\sin$  is (+) in Q1 + Q2  $(-x, 2/3)$  

$$\theta = \pi - 0.73 = \underline{2.41 \text{ rad}}$$

$$\boxed{\{0.73, 2.41\}}$$